

## HOMEWORK 10, CALCULUS AND LINEAR ALGEBRA, 2015/2016

Assigned 12/02/2015, due 12/09/2015, collected from 2pm to 2.15pm sharp!

Name and Family Name (CAPITAL LETTERS): \_\_\_\_\_

MATRICOLA N.: \_\_\_\_\_

**Exercise 1**

Consider the matrix  $A = \begin{pmatrix} 1 & 0 & 1 \\ -2 & 1 & 0 \\ 3 & 2 & 0 \end{pmatrix}$ .

- a) Compute the determinant of  $A$  using the Laplace method.
- b) If possible, compute the inverse matrix of  $A$ .
- c) Using the matrix method, solve the following linear system

$$\begin{cases} x + z = 1 \\ -2x + y = -1 \\ 3x + 2y = 0 \end{cases}$$

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## Exercise 2

Consider the matrix  $A = \begin{pmatrix} 1 & 2 & 1 \\ 6 & -1 & 0 \\ -1 & -2 & -1 \end{pmatrix}$ .

- a) Compute the eigenvalues of  $A$ .
- b) Compute the associated eigenvectors with length 1.
- c) Consider the vector  $\vec{v} = \frac{2}{\sqrt{6}} \begin{pmatrix} -1 \\ 2 \\ 1 \end{pmatrix} + \frac{1}{\sqrt{17}} \begin{pmatrix} 2 \\ 3 \\ -2 \end{pmatrix}$ . Compute the product  $A\vec{v}$  using the previous results.